

# Space Debris and Collision Risk in the Orbital Commons

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# Motivation

# Research questions

# What do we know?

# Framework

- Satellite and debris accumulation,

$$S_{t+1} = S_t(1 - L(S_t, D_t)) + X_t$$

$$D_{t+1} = D_t(1 - \delta) + G(S_t, D_t) + \mu_L X_t$$

- Discrete time dynamic optimization: launch today if discounted stream of satellite returns starting tomorrow is larger than the launch cost
- Perfect competition, constant returns, immortality, and open access
- We compare open access to a sole owner of the entire fleet
- Kessler syndrome is occurring if  $\kappa(D_t) > 0$ , where

$$\kappa(D_t) = -\delta D_t + G(0, D_t)$$

# A firm's problem

Words

Equilibrium condition

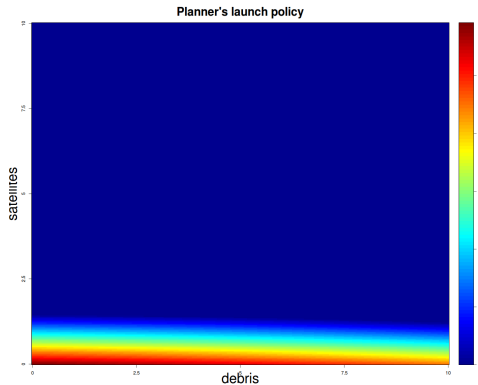
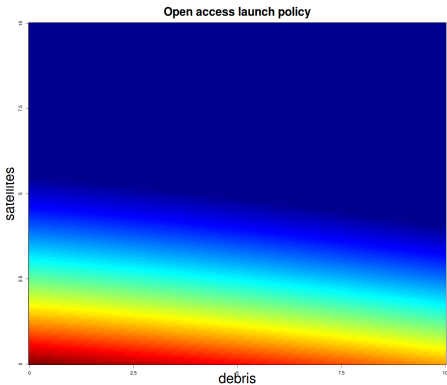
# The fleet owner's problem

Words

Optimality condition

# Open access and optimal incentives to reduce congestion

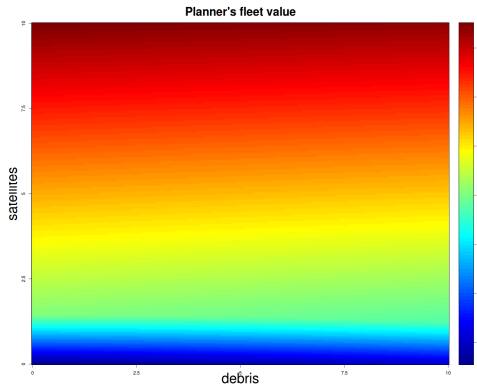
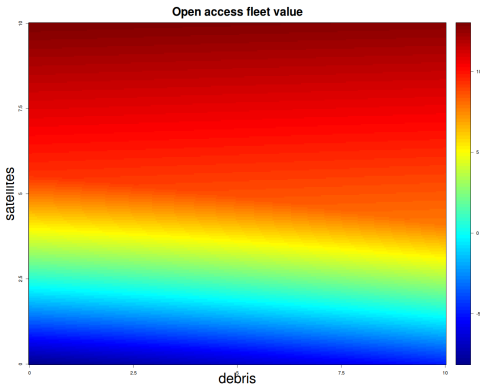
Open access firms respond to risk, but not optimally: they don't internalize the risks their own satellites pose





# Open access and optimal incentives to reduce congestion

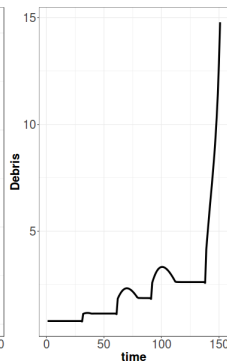
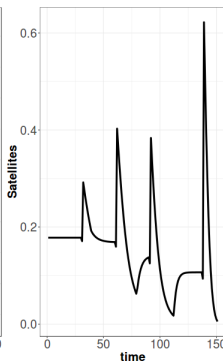
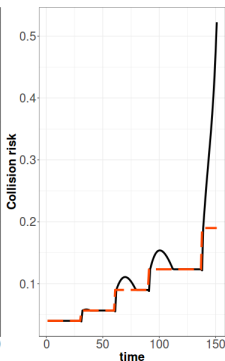
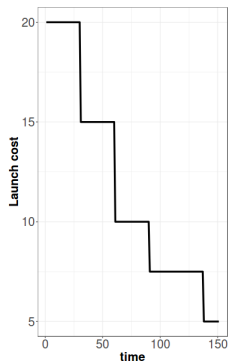
Open access fleets are too large and not as valuable; higher debris stocks are costlier



# Lower costs and Kessler syndrome under open access

## Proposition 10

All else equal, sustained decreases in launch costs will eventually cause Kessler syndrome



# Lower costs and Kessler syndrome under open access

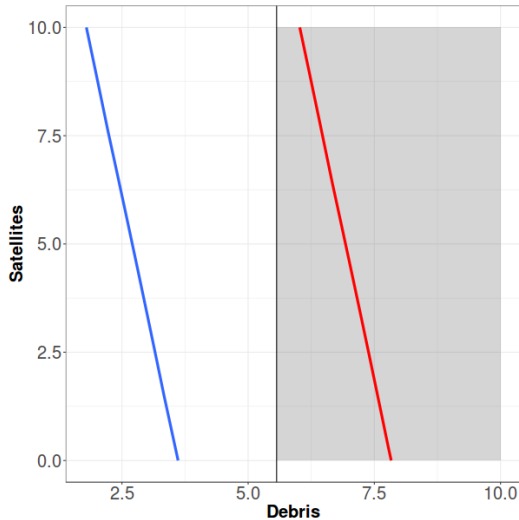
*Open access:* Launch until  
risk = excess return

Launch cost ↓

⇒ excess return ↑

⇒ eqm set shifts →

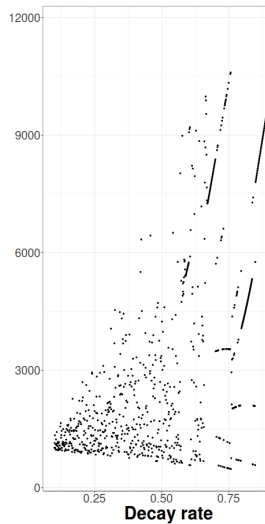
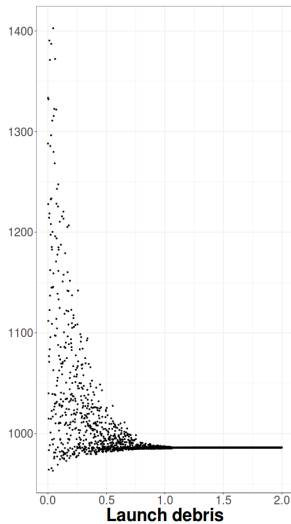
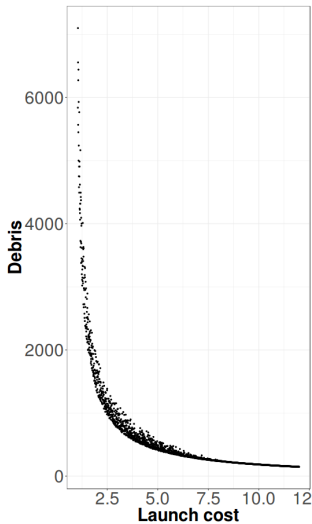
Eqm set will eventually be  
pushed to Kessler region



# Open access dynamics: instability

../images/decay\_increase\_1.png

# Open access dynamics: instability



# Orbit management is an economic problem

- ① Launch rates and debris are endogenous
  - Modeling debris with exogenous launch is looking at the symptoms and ignoring the cause
- ② Open access is an inefficient way to manage orbits
  - Not just debris, too many satellites
- ③ Congestion creates incentives to limit debris growth, but not enough
  - Open access can cause Kessler syndrome in LEO

Thank you!

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